

Duplication for publication or sale is strictly prohibited

Without prior written permission of

The Transportation Research Board

**CAPACITY ANALYSIS FOR BIFURCATED ESTUARIES  
BASED ON SHIP DOMAIN THEORY AND ITS APPLICATIONS**

**Xingjian Zhang**

School of Navigation, Wuhan University of Technology,  
Wuhan 430063, China

**Junmin Mou**

Hubei Key Laboratory of Inland Shipping Technology,  
Wuhan University of Technology, Wuhan 430063, China.

**Jianfeng Zhu**

**Pengfei Chen**

School of Navigation, Wuhan University of Technology,  
Wuhan 430063, China;

**Rongfang (Rachel) Liu**

New Jersey Institute of Technology,  
University Heights, Newark NJ 07102  
Tel: 973-596-5884 Fax: 973-596-5790  
Email: [rliu@njit.edu](mailto:rliu@njit.edu)

**Submitted to**

**Transportation Research Board  
For  
Presentation and Publication**

Initial Submission: July 2016

Revised Submission: November 2016

1 **ABSTRACT**

2 The bifurcated estuary is an important segment of increasingly important marine transportation  
3 systems. Due to branching channels, cyclical change of water levels, and sophisticated operating  
4 rules in many large bifurcated estuaries, it is often difficult to estimate the traffic capacity and  
5 simulate the ship motions, even though it is critically important for traffic management and  
6 efficiency. In recent years, the increasing number of ships that collect and contribute to the  
7 Automatic Identification System (AIS) have made it possible to monitor traffic flow along  
8 waterways, including bifurcated estuaries.

9

10 This study developed a typical capacity estimation model based on ship domain theory. Utilizing  
11 AIS data collected in the Yangtze River Estuary, a typical Bifurcated Estuary System, the authors  
12 have analyzed various physical characteristics, weather conditions, and vessel characteristics in  
13 order to derive related impacts of each on overall capacity of the bifurcated estuary. Validated  
14 with practical observations, the method can be applied to similar estuary fairway systems to  
15 improve waterway operations and management.

16 **KEYWORDS**

17 Capacity analysis, AIS, bifurcated estuary, ship domain theory

18 **WORD COUNTS:**

19 4,055 + 4 tables + 8 figures = 7,055

20

# 1. INTRODUCTION

Estuarine waters, as an essential element of waterway network, play a significant role in the development of a maritime economy. More than two-thirds of the largest cities in the world are located at the estuaries of respective rivers (Ross, 1995). With continuous development of domestic and international economic activities, the number and size of ships have been growing continuously. As a result, the density of water traffic is much more condensed than before, especially in the estuarine waters, which causes higher demand for continuously increased utility of waterway capacity.

Given limited capacity in estuary waters and the large investment required to develop and maintain estuary channels, it is important to evaluate the existing capacity, plan future improvement, and manage or optimize waterway capacity, which are all built on the accurate estimate and forecast of the capacity of the estuary channels. However, as the transition zone between the river and the marine environment, estuaries are often subject to the influences of ocean such as tides, waves and influx of saline water, and of rivers such as flows of fresh water and sediment. Complicated by the geomorphological characters, weather conditions, and variations of bifurcated channels, the capacity analysis for bifurcated estuary waterways is very different from that of conventional inland waterways.

Since the implementation of the Automatic Ship Identification System (AIS), it has been possible to track the movements of a large number of ships in various locations by AIS data mining and advanced computation ability. Also, the real-time records of weather, wave, and tidal situations have provided a better platform to isolate and quantify the impact of each factor. These developments can facilitate studies of waterway capacity. However, there are few studies to evaluate the capacity of the bifurcated estuary waterways by AIS data mining.

1 To fill this gap and improve the capacity in estuarine waters, this study has developed a  
2 theoretical framework based on the ship domain theory and AIS data available to estimate the  
3 vessel capacity of bifurcated estuary waterways. The major contribution of this study is the  
4 application of a theoretical model proposed by Wu and Zhu to the Yangtze River Estuary, the  
5 largest estuary waterway network in China, taking full advantages of AIS data available. The  
6 estimation of the capacity of the Yangtze River Estuary is in agreement with the observations  
7 from 2013 and 2014. The content of this paper is as follows: Section 2 provides a description of  
8 the research background. Section 3 elaborates the formula of capacity analysis and method to  
9 compute the standard ship domain. Section 4 focuses on the Yangtze Estuary Waterways as a  
10 case study. The related parameters in the ship domain model are determined based on AIS data  
11 and sea-weather information from the Shanghai Maritime Safety Administration. Section 5  
12 highlight the findings of this study and points out future research directions.

## 13 **2. RESEARCH BACKGROUND**

14 The capacity analysis is critically important as it is the foundation of the effective operation  
15 and management of waterway systems. Many scholars have developed theoretical frameworks  
16 and modeling approaches for conventional inland waterways, which are the prerequisite to the  
17 research on bifurcated estuary waterways. For example, Dian (2000) studied the traffic capacity  
18 of inland waterways in the low-water season based on the vessel traffic flow, and calculated the  
19 maximum capacity of a standard ship. Li (2006) studied the design traffic capacity of inland  
20 waterways and provided corresponding calculation methods and classification standards for  
21 various levels of services. Liu (2006) identified three main factors: the speed of the traffic flow,  
22 the ship domain, and the channel width, affecting the capacity of the congested inland  
23 waterways. Focused on the problem of the maximum capacity, Duan (2012) constructed a  
24 theoretical model regarding traffic capacity of network channels, which was based on the  
25 network topological structure of water-network channels and the basic characteristics of

1 navigation as well as Space-time Consumption Theory. The idea capacity are modified by  
2 correction factors with which the characteristics of vessel traffic in waterways can be reflected.  
3 Generally, these models follow a similar form described in Equation (1):

$$4 \quad C = n \cdot v \cdot \frac{1000}{L + D} \cdot \prod \alpha_i \quad (1)$$

5 Where:

- 6  $n$ : number of traffic lanes;
- 7  $v$  : ship's operation speed;
- 8  $L$  : ship length;
- 9  $D$  : safe distance of vessels; and
- 10  $\alpha_i$  : correction factors.

11  
12 Due to the influence of the kinetic dynamics of the river and the adjacency between estuary and  
13 ocean, the flow pattern of an estuary is typically a fork-shaped split. In mesh grids, the water  
14 channels in the estuary region often form unique flow patterns with various depths and widths,  
15 which may render traditional traffic flow models and/or capacity analyses futile, inaccurate or  
16 inadequate for application.

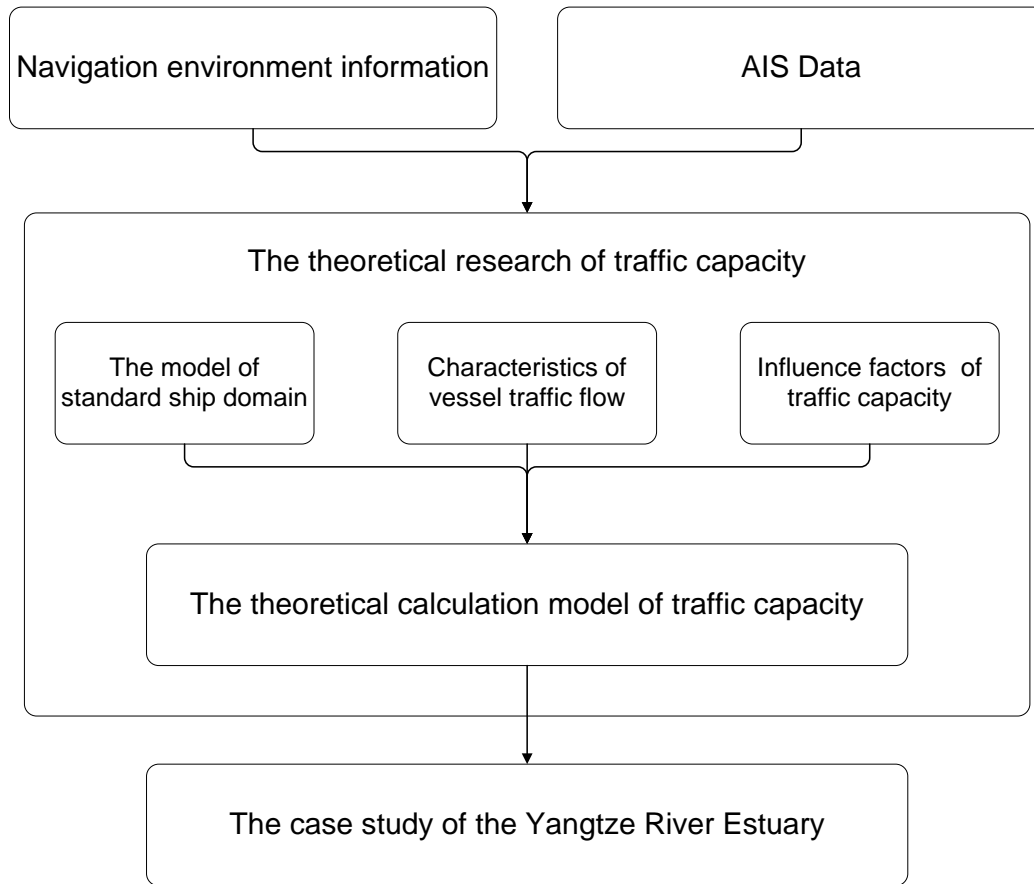
17  
18 To improve the conventional traffic flow vessel capacity analysis for inland waterways, we  
19 investigated the origins of the Ship Domain Theory (SDT). First defined by Japanese scholars  
20 (Fujii and Tanaka 1963), SDT dictates an effective area around a ship that a navigator would like  
21 to keep clear with respect to other ships or stationary objects in order to ensure the safe  
22 operations of the vessels. SDT is one of the most effective theories to describe and estimate  
23 vessel traffic and ship behavior (Wu and Zhu 2004).

24  
25 Since the original establishment of an ecliptic model of ship domain by SDT, quite a few  
26 researchers have established many models of ship domains with different shapes and sizes

1 including the oval, round and polygon (Wang 2010, Liu and Wu 2011, Qi and Li 2011, and Xu et  
2 al 2004). Prior to the implementation and application of the AIS System, research on ship  
3 domains developed slowly and was restricted by vessel information. With the recently aggressive  
4 promotion of the AIS system, it is now possible to acquire massive, accurate, and real-time  
5 vessel data and movement information (Mou, Tak, and Ligteringen 2010). Erwin (2012)  
6 developed ship domain boundaries by plotting distances and relative direction between the target  
7 and reference ships. By eliminating certain ratios of the reference ship versus the subject ship,  
8 Erwin has developed the most representative ship domain dimensions. Ren (2013) established a  
9 model of dynamic ship domain by using recently collected AIS data. However, limited by the  
10 AIS data available, the boundaries of the model are still rough. Hansen (2013) found that the  
11 establishment of an empirical minimum ship domain related to a comfortable navigational  
12 distance via analyzing AIS data. Tu (2016) surveyed AIS data sources and relevant aspects of  
13 navigation in which such data could be exploited for collision prediction based on Ship Domain  
14 Theory

15

16 Based on the concept of ship domain theory and the lack of development in capacity analysis for  
17 bifurcated estuary waterways, this manuscript documents a dynamic model that is suitable to  
18 estimate the capacity of bifurcated estuary waterways. The framework of the model is illustrated  
19 in Figure 1. Detailed concept and mathematical equations are introduced in Section 3.



1  
2

Figure 1. The framework of the model

### 3. CAPACITY ANALYSIS

4 Similar to the capacity analysis for surface transportation modes, the basic principle in the  
5 capacity analysis for marine transportation is largely based on the density of the vessels and their  
6 speeds. What is different from the conventional surface transportation is that the waterway  
7 channel delineation is much more fluid than the lane marking direction division. Such fluidity is  
8 further compounded and various in the bifurcated estuary region.

9

#### 10 *3.1 The Basic Model*

11 Applying a basic traffic engineering principle to the unique characteristics of bifurcated estuary  
12 waterways, capacity is defined as the maximum throughput passing a given point of the

1 waterway channel in a given unit of time, such as an hour, a day or a month. The ideal capacity  
2 may be affected by various geomorphological, weather, and operation regulations, which are  
3 reflected as modification factors. However, a mathematical model for estimating the capacity of  
4 waterways has been proposed by Wu and Zhu, shown in Equation (2). We follow this model to  
5 describe the basic throughput for bifurcated estuary waterways.

$$C_p = \eta \cdot W \cdot \rho_{\max} \cdot v = \eta \cdot W \cdot \frac{1}{r \cdot s} \cdot v \quad (2)$$

7 Where

8  $\eta$ : modification factor;

9  $W$ : The width of the fairway;

10  $\rho_{\max}$ : Maximum ship density per unit length fairway;

11  $r \cdot s$ : Long and short axis of the standard ship domain;

12  $v$ : the speed of the vessel.

13

14 The modification factor is a product of many composite impacts from wind, fog, wave, and other  
15 nature conditions and is unique to a particular estuary. The width of the estuary channels may  
16 vary along the horizontal profile but remains stable for a given cross section. Another important  
17 factor is the ship domain, an oval denoted by the long axis— $r$ , and the short one— $s$ . The speed  
18 of the vessels is usually controlled by the channel conditions in the estuary, bounded by a low  
19 and high range, and generally collected in the AIS database.

20

### 21 ***3.2 Standard Ship Domain***

22 There are many different ways to derive the dimensions of a ship domain. This approach  
23 measures the distance between the subject ship and adjacent ones. After plotting the relative  
24 positions for the target ship and surrounding ones, this study delineated the boundaries of the  
25 ship domain by excluding certain extreme values.



1  
2 Analyzing all around ships is critical for the precision of our estimation, but due to the huge  
3 calculating burden and mountainous AIS data, we have divided the proximity of the target ship,  
4 360 degrees, into 72 equal sectors, using 5 degrees as the step size in the computer-calculation  
5 program. The total number of ships in each sector is tallied and the distances between the target  
6 ship and surrounding ones are measured. Using a large quantity of ship positions collected in the  
7 AIS database, the authors have plotted the critical points of each sector and connected them into  
8 a closed polygon which is the size and shape of the ship domain for the target ship.

#### 9 **4. CASE STUDY**

10 Many bifurcated estuary waterways play significant roles in transporting people and goods for  
11 large cities around the world. Each estuary is unique not only because of the geomorphological  
12 features, but also the traffic flow patterns, historical development, and vessel characteristics. The  
13 approach to calibrate capacity or maximum throughput is often associated with a particular  
14 bifurcated estuary region. In this case, the Yangtze River Estuary was chosen as a case study.

15

##### 16 ***4.1 The Yangtze Estuary Waterways***

17 As the longest and largest river in China and the third in the world, the Yangtze River has not  
18 only nurtured Chinese civilization from ancient times but also gathered the largest number of  
19 inland ports in China. Since its origination in the high mountains and plateaus of Sichuan  
20 province in southeast east China, the Yangtze river has traversed more than two thousand miles  
21 when it meets the ocean in the middle of the eastern China seaboard. As one of the largest  
22 bifurcated estuary systems, the Yangtze Estuary waterways have two main channels: the  
23 northern channel and the southern one as depicted in Figure 2.

1  
2 **Figure 2. Yangtze River Estuary**  
3

4 Due to its close proximity to Shanghai, the most powerful economic engine in China today, the  
5 Yangtze River Estuary waterways have been used by a large number of vessels of tremendous  
6 size and cargo loads. As shown in Figure 3, the vessel types in both northern and southern  
7 channels have been dominated by generally large cargo ships. With slightly deeper channels, the  
8 northern waterway has had an even higher share of general cargo ships, and the southern channel  
9 caters to a larger share of passenger ships.

10  
11 The length of the vessels is generally concentrated at the longer end, between 90 to 180 meters  
12 and some of them longer than 180 meters as shown in Figure 4. Comparing the distributions of  
13 the vessel length in both channels, it seems that the southern channel has the largest share of  
14 larger ships between 90 to 180 meters while the northern channel accommodated more of the  
15 largest ships, over 180 meters in length. The travel speed of those vessels in both waterways  
16 ranges from 8 to 16 kn. The speed distribution in both channels follows a normal distribution but  
17 with the northern channel skewed more toward the higher speed. For example, the large share of  
18 speed for the northern channel is between 14-16 kn while the southern channel 10-12 kn. It is  
19 rare but there is a small percentage of vessels that travel above 20 kn.

1

2

3

**Figure 3. Vessel Type Distributions**

1  
2

**Figure 4. Distribution of Ship Length**

3  
4

**Figure 5. Distribution of Ship Speeds**

1 **4.2 Typical Ship Domain for the Yangtze River Estuary**

2 Given the higher share of large cargo ships with a typical length of 90 to 180 meters as shown in  
3 Figure 3 and Figure 4, a general cargo ship, ranging in length from 90 to 180 meters, is the  
4 standard or typical ship chosen as the basis for ship domain estimation. Applying the approach  
5 presented in Section 3, the ship field has been divided into 72 equal sectors and the distances  
6 between the target ship and adjacent reference ships were plotted

7  
8 Utilizing the AIS data for the past three years, the detailed locations of more than 150,000  
9 vessels have been plotted according to the methodology introduced in Section 3. As shown in  
10 Figure 6, a typical ship domain was derived for the northern and southern fairways respectively.  
11 Confirming to the predictions by Fujii and Tanaka, the standard ship domain is very similar to an  
12 ellipse with long axis tilted to the right slightly. Using a 95% confidence interval, the boundary  
13 values for the long axis of a standard ship domain in the northern fairway is about 10 times the  
14 ship length, and the short axis 4 times the ship length. If the 99% confidence interval is applied,  
15 the boundary values for the long axis of the standard ship domain in the northern fairway  
16 becomes 6 times the ship length and the short axis 3 times the ship length. Detailed boundary  
17 values for both long and short axes for the northern and southern fairways are listed in Table 1.  
18 The experiment values fall well into the range of 3-8 times the ship length for the long axis and  
19 1.6 times the ship length for the short axis, which are provided in existing literature. But the  
20 actual derivation of the specific typical ship domain for the northern and southern fairways  
21 respectively provided researchers a highly accurate base for further capacity analyses.

22 **Table 1. Typical Ship Domain**

confidence coefficient	Northern Fairway	Southern Fairway
95%	$10L \times 4L$	$8L \times 3L$
99%	$6L \times 3L$	$6L \times 2L$

1

2

3 **Figure 6. Standard Ship Domain for Northern and Southern Fairways**

4

5 ***4.3 Ship Density Calculations***

6 Regarding ship domains, the travel speed is another important characteristic that affects the  
7 capacity or throughput of a particular waterway. The speed distribution in both northern and  
8 southern channels has been tested using a KS test and normal fitting curves as demonstrated in  
9 Figure 7. As mentioned before, the speed distribution for the southern fairway follows a typical  
10 normal distribution while the northern fairway skewed toward the higher speed categories. The  
11 larger concentration of vessel speed around 14-16 kn and the very small share for all speed  
12 categories greater than 16 kn is caused by the traffic control regulations.

13

1 Given the skewed distribution of speed in the northern fairway, the typical or standard speed  
2 cannot be represented by a simple mode, mean or average value alone. A statistical analysis of  
3 the speed profile for the northern fairway was performed and presented in Table 2. To avoid  
4 abnormal value, the derived median speed, 12.3 kn and 11.1 kn for vessels traversing the  
5 northern and southern fairways respectively, is used to substitute the “v” in Equation 2.

6

7

8

### **Figure 7. Normal Fitting of Speed Distributions**

1

2

**Table 2. The Statistical Analysis of Speed Distributions**

	Northern Fairway	Southern Fairway		Northern Fairway	Southern Fairway
mean	11.8	10.9	kurtosis	179.66	272.0541
median	12.3	11.1	minimum value	1.7	0.3
mode	14.8	11.9	maximum value	26.9	26.8
Standard deviation	4.33	3.75	observed value	2119	3852
variance	18.71	14.08	Confidence (95.0%)	0.18	0.12

3

4 The width,  $W$  denoted in Equation 2, represents the width of waterway channels. In the Estuary  
5 context, the width of the channel is often increasing when approaching the ocean. However,  
6 given the traffic management conditions, the traffic flows are usually divided in two directions;  
7 therefore,  $W$  can be simplified as two times the short axis of the ship domain ellipse.

8

9 Given the diversified ship length, shape and operating characteristics, a statistical analysis was  
10 also performed to identify the typical ship length to be used to calculate capacity in bifurcated  
11 estuary channels. Applying the same approaches presented earlier, Shanghai Maritime Safety  
12 Administration has developed and adopted a set of conversion factors to identify a typical or  
13 standard ship. As presented in Table 3, the same conversion factors were applied and the typical  
14 ship length was identified as 175 and 121 meters for the northern and southern channels,  
15 respectively.

16

17 Once the standard ship domains are determined, it is straightforward to derive the ship density,  
18 which was included in Equation 2. Bringing the values of long and short axes of an ellipse to the



density function  $\rho_{max}$ , the ship density was calculated for both northern and southern fairways for both 95% and 99% boundary conditions.

**Table 3 Conversion Factor of Standard Ship (MSA of Shanghai)**

The Length of Ship (m)	<30	30~50	50~90	90~180	>180
Conversion Factor	0.30	0.50	1.00	2.00	3.50

Proportion of ships in different lengths					
The Length of Ship (m)	<30	30~50	50~90	90~180	>180
Northern Fairway (%)	2.95%	1.19%	0.54%	56.50%	38.82%
Southern Fairway (%)	6.32%	1.64%	19.64%	67.92%	4.48%

#### 4.4 Modification Factors

Once all the parameters are estimated, the maximum capacity under ideal conditions can be calculated. However, the real world operations of inland or estuary waterways are far from perfect or ideal. The maximum capacities are often modified or impacted by weather conditions such as wind, wave, fog, and uneven distribution of vessel fleets. For example, there were 117 days in 2010 when the wind reached level 7 on the Beaufort scale; the wind speed was greater than 13.9 m/s, the ability of navigation was blocked; therefore, the capacity of the fairways was reduced to zero. Similarly, when the visibility is less than 1000 meters, no vessel is allowed to travel along the deep waters of the northern channel which reduces the throughput of the channel significantly. Table 4 presents the values of modification factors.

**Table 4. Modification Factors**

Modification Factors					
$\eta_f$	$\eta_w$	$\eta_h$	$\eta_y$	$\eta_s$	$\eta$
0.885	0.904	0.993	0.85	0.9	0.608

1 **4.5. The Capacity Calculations**

2 Applying the ship domain dimensions, speed distribution, and typical ship length derived from  
3 AIS data for the Yangtze estuary channels, the maximum capacity was derived for the northern  
4 and southern channels under ideal conditions. Further modified by the modification factors  
5 provided by the local marine management authority, the estimated maximum capacities for the  
6 northern and southern channels are 159,432 and 259,296 vessels per year respectively. The total  
7 throughput when both directions are combined is about 418,728 vessels per year.

8

9 Comparing the maximum capacities for both northern and southern channels with their  
10 respective observed throughput in the past three years, utilization rates for both channels can be  
11 derived. As presented in Figure 8, the traffic volume in the northern channel is fairly stable,  
12 hovering around 36 percent of the saturated capacity. The traffic volume in the southern channel  
13 experienced significant growth since 2011, and it reached almost 57 percent in 2014.

14

15 These facts could be possibly explained by the reason that a number of large projects, such as a  
16 10.5-meter channel and 12.5-meter channel development had been invested in the pipelines.  
17 Compared with the actual data, the calculated capacity of the Yangtze River Estuary channel can  
18 meet current requirements, and there is still a large increase in the number of vessels. Accurate  
19 and timely estimation of the throughput for bifurcated estuary channels is the basis for planning  
20 long-term investment, optimizing operations, and improving water conditions in the near future.

21

1  
2 Figure 8. Volume to Capacity Ratio for Northern and Southern Channels  
3

## 4 **5. CONCLUSION**

5  
6 The capacity estimation process documented in this manuscript took advantage of a large amount  
7 of AIS data collected in a particular location. The ever-increasing contributions and  
8 accumulations of AIS data and computation approaches will provide great opportunities to a  
9 further improvement in the ship domain estimation, which is useful not only for the safe  
10 movements of vessels but also maximization of capacity and/or optimization of marine  
11 transportation operations.

12  
13 In the next-step research, more complicated methodologies for the ship domain in this estuary  
14 will be discussed. Moreover, the AIS data will be collected and evaluated for a more accurate  
15 estimation. Based on accurate capacity estimation, Maritime Administration may develop long  
16 range waterway plans, improve operations and ensure and/or improve the safety and efficiency  
17 of waterway systems.

1 **REFERENCES**

2

3 Erwin van Iperen. 2012. Detection of Hazardous Encounters at the North Sea from AIS Data.  
4 Maritime Research Institute Netherlands. The Netherlands, 2012.

5

6 Ross, D.A. 1995. Introduction to Oceanography. New York: Harper Collins College Publishers.  
7 ISBN 978-0-673-46938-0.

8

9 Fujii Y, and Tanaka K. 1971. Traffic capacity. Journal of Navigation. 1971. 24 (04):543-552.

10

11 Bian, Yijie. A Study on Waterway Transit Capacity. Port & Waterway Engineering 2000, 08:27-  
12 30+48.

13

14 Li, Ying. 2006. Research and Application on Waterway Transit Capacity. HoHai University,  
15 2006.

16

17 Liu, Shaoman. 2006. The Research of the Inland River Channel Transit Capacity. Dalian  
18 Maritime University.

19

20 Duan, Lihong. 2012. Calculation Model of Water-network Channel Transit Capacity Based on  
21 Theory of Space-time Consumption. Ship & Ocean Engineering. 2012, 05:134-137.

22

23 Liu, Shaoman and Zhaolin Wu, 2011. The Research Summary of Ship Domain. Journal of Dalian  
24 Maritime University. 2011(01):51-54

25

26 Mou, J. M.,Tak, C. and Ligteringen, H. 2010. Study on Collision Avoidance in busy fairway by

1 Using AIS Data. *Ocean Engineering*, 2010, 37:483-490.

2

3 Qi, Le and Guopin Li. 2011. AIS-data-based Ship Domain of Ships in sight of one another.

4 *Journal of Dalian Maritime University*. 2011(01):48-50

5

6 Ren Yalei. 2013. Study on Ship Encounters Using AIS-Data. Wuhan University of Technology.

7 2013.

8

9 Hansen M G, Jensen T K, Lehn-Schiøler T, et al. 2013. Empirical ship domain based on AIS

10 data. *Journal of Navigation*, 2013, 66(06): 931-940.

11

12 Tu E, Zhang G, Rachmawati L, et al. 2016. Exploiting AIS Data for Intelligent Maritime

13 Navigation: A Comprehensive Survey. arXiv preprint arXiv:1606.00981, 2016.

14

15 Wang, N. 2010. An Intelligent Spatial Collision Risk Based on the Quaternion Ship Domain.

16 *Journal of Navigation*. 2010, 63:733-749.

17

18 Wu, Zhaolin and Jun Zhu. 2004. *The Maritime Traffic Engineering*. Dalian Maritime University,

19 2004.

20

21 Xu, Zhouhua, Junmin Mou, and Yongqin Ji. 2004. A Study of 3D Model of Ship Domain for

22 Inland Waterway. *Journal of Wuhan University of Technology, Transportation Science&*

23 *Engineering*. 2004 (03).

24

1 **ACKNOWLEDGEMENTS**

2 The work presented in this paper is financially supported by the National Nature  
3 Science Foundation of China (Grant No.51579201).

4

5

6

7

8

9

10

11

12

13

14

15

16

17